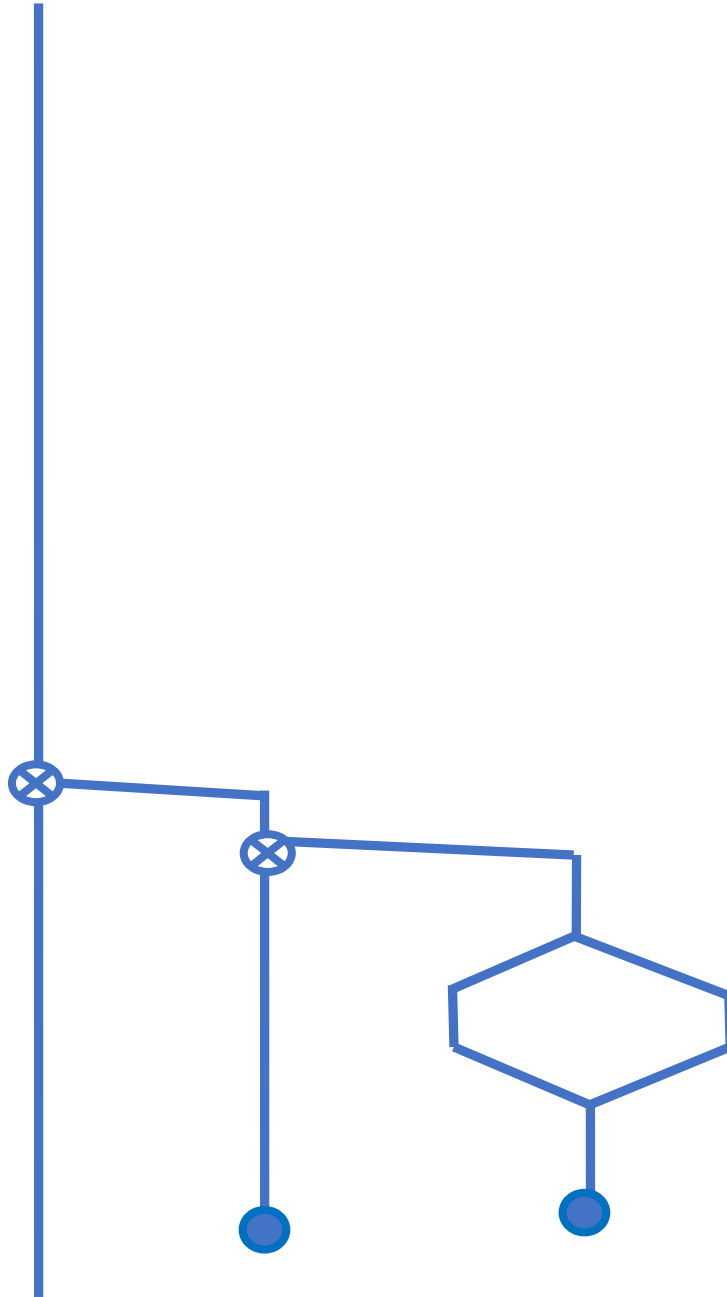


The Road Trip Conjecture

SVFIG

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Awareness

During a recent lunch, I saw on the table the formula:

$$111,111,111 * 111,111,111 =$$
$$12,345,678,987,654,321$$

And decided to investigate it.

The Conjecture

I know 1 squared is 1.

I know 11 squared is 121.

It is likely 111 squared is 12321.

Does that pattern hold for all similar squares up to 12,345,678,987,654,321

I decided to investigate it.

Discoveries

- I wrote the full program thinking it was done.
- Big surprise and learning experience.
- There is no double number multiply in Win32Forth.
- There is a single x single to double. M^*
- There is an interesting unsigned double-number formatted print with commas. UD,.R.

Support Words

```
: Msquare ( n1 — d1 ) \ Square single n1 to double d1.  
  dup M* ;
```

```
: increment ( n1 — n2 ) \ Shift and append a '1'.  
  10 * 1 + ;
```

Driving Program

```
: main ( -- ) \ incrementing squares
    1          \ initial value
    9 0 do
        dup s>d    cr 14 ud,.r
        dup Msquare 25 ud,.r
        increment loop
    1- 10 / Msquare cr cr 39 d.r ;
```

Results

1
11
111
1, 111
11, 111
111, 111
1, 111, 111
11, 111, 111
111, 111, 111

1
121
12, 321
1, 234, 321
123, 454, 321
12, 345, 654, 321
1, 234, 567, 654, 321
123, 456, 787, 654, 321
12, 345, 678, 987, 654, 321

12345678987654321 ok

Q.E.D

