



Quantum Encryption

FPGA Integration



Incorporating FPGA Chips as Security Keys in Quantum Encryption

- Field-Programmable Gate Arrays (FPGAs) are highly versatile, programmable silicon chips that can be configured to perform a wide array of computing tasks. Their reprogrammable nature, high-speed processing capabilities, and parallel processing features make them an ideal choice for a variety of applications, including cybersecurity. When combined with quantum encryption methods, FPGA chips can significantly enhance the security and efficiency of cryptographic protocols.



Integration of FPGA Chips in Quantum Encryption

- **Quantum Key Distribution (QKD) Acceleration:**
- **Key Generation:** FPGA chips can rapidly process quantum measurement outcomes to generate encryption keys. Their ability to handle parallel computations allows for the fast generation of keys, which is essential in real-time communications.
- **Error Correction and Privacy Amplification:** After the initial key generation phase in QKD, certain post-processing steps like error correction and privacy amplification are required. FPGAs can efficiently execute these computationally intensive tasks, ensuring the final key is secure and free from any potential eavesdropping.



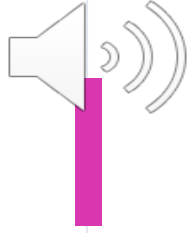
Simulation and Real-time Processing:

- **Quantum Circuit Simulation:** For development and testing purposes, FPGAs can simulate quantum circuits much faster than conventional processors, providing a platform for testing quantum encryption algorithms before they are run on actual quantum hardware.
- **Real-time Quantum Encryption:** In a deployed system, FPGAs can process quantum encryption algorithms in real-time, ensuring that data encryption and decryption are performed with minimal latency.



Secure Key Storage:

- **Hardware-based Security:** FPGA chips can securely store encryption keys and perform cryptographic operations directly on the chip. This hardware-based approach to key management enhances security by minimizing the exposure of sensitive keys to potentially compromised software environments.



Custom Cryptographic Protocols:

- **Customization and Flexibility:** The programmable nature of FPGA chips allows for the implementation of custom, proprietary cryptographic protocols or the optimization of existing ones to meet specific security requirements or performance metrics.
- **Adaptability:** As quantum-resistant encryption algorithms evolve, FPGA chips can be reprogrammed with new algorithms, ensuring the cryptographic system remains secure against emerging threats.

The Not So Hard Stuff Quantum Gates

Quantum gates typically included in a quantum computing library, such as Qiskit. These gates operate on qubit states, which are vectors in a complex Hilbert space and for this example it is a space where there are infinite positions where the gate is stored in the FPGA. Here, we'll focus on single-qubit gates for simplicity.

$$Y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$$

$$X = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

$$Z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

Pauli-X Gate (NOT Gate) The not gate is an entry way to say hay I am here let's start.

1. Pauli-X Gate (NOT Gate)

The Pauli-X gate is the quantum equivalent of the classical NOT gate. It flips the state of a qubit:

$$X = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

Applied to a qubit state, it transforms $|0\rangle$ to $|1\rangle$ and $|1\rangle$ to $|0\rangle$.

**Pauli-Y Gate Do you Spin me Round and Round.
This sets the position of the gate direction. Hey, go in this direction.**

2. Pauli-Y Gate

The Pauli-Y gate rotates a qubit state around the Y-axis of the Bloch sphere by π radians:

$$Y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$$

It introduces a phase shift in addition to flipping the qubit state.

3. Pauli-Z Gate (Phase Flip Gate) Lets Flip It to name the user and find the direction of the Not Gate. It uses radians a degree of direction but unchanged because it recognizes the user not gate and y gate.

3. Pauli-Z Gate (Phase Flip Gate)

The Pauli-Z gate flips the phase of the qubit state $|1\rangle$ without changing its amplitude:

$$Z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

It leaves $|0\rangle$ unchanged but maps $|1\rangle$ to $-|1\rangle$.

Hadamard Gate This is important we recognize you and we are sending you with this password that is encrypted

4. Hadamard Gate

The Hadamard gate creates a superposition state from a definite state. It is represented as:

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$$

It transforms $|0\rangle$ to $\frac{|0\rangle+|1\rangle}{\sqrt{2}}$ and $|1\rangle$ to $\frac{|0\rangle-|1\rangle}{\sqrt{2}}$.

T Gate (T-Phase Gate)

We are going to confuse you now that you have the credentials so no one follows you.

6. T Gate (T-Phase Gate)

The T gate is a more subtle phase shift, applying a phase of $\pi/4$:

$$T = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{pmatrix}$$

Like the S gate, it does not change $|0\rangle$ but maps $|1\rangle$ to $e^{i\pi/4}|1\rangle$.

CNOT Gate (Controlled-NOT Gate) We are now going to encrypt those previous steps go back to the beginning. We are using a matrices of suppositions ie spins that are quantum that classical computers can not compute or calculate.

7. CNOT Gate (Controlled-NOT Gate)

While not a single-qubit gate, the CNOT gate is fundamental in quantum computing for entangling qubits. It is represented as:

$$\text{CNOT} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$

The CNOT gate flips the second (target) qubit if the first (control) qubit is in state $|1\rangle$.

Let's calculate the effect of applying a Hadamard gate to a qubit initially in the state $|0\rangle|0\rangle$, a common operation in quantum computing that illustrates the creation of a superposition state. Simply, multiply the groups like the foil method and using cosine as the square root. Find the angle in ie gate with sq root. It will give the gate key in a spin phase ie supposition.

Initial State: $|0\rangle$

In quantum computing, the state $|0\rangle$ can be represented as a vector:

$$|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

Hadamard Gate

The Hadamard gate, represented by the matrix H , is defined as:

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$$

Applying the Hadamard Gate to $|0\rangle$

To apply the Hadamard gate to $|0\rangle$, we multiply the H matrix by the $|0\rangle$ vector:

$$H|0\rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

Let's perform this matrix-vector multiplication:

$$H|0\rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \times 1 + 1 \times 0 \\ 1 \times 1 + (-1) \times 0 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

The result is:

$$H|0\rangle = \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

Secure Gate Key Generation, Make it safe

- **Complexity and Unpredictability:** By abstracting quantum gate operations into mathematical models involving π cosine constants and applying these in an n th integer superposition framework, you create a layer of complexity and unpredictability that is hard to replicate without knowing the exact parameters and algorithms used. This unpredictability is a cornerstone of cryptographic security.

Key Sharing

- Key Sharing:
- Alice transmits the key to Bob through a secure channel established by the FPGA. The FPGA uses its hardware capabilities to encrypt the transmission further, perhaps using a physically unclonable function (PUF) for an additional layer of security.



Communication

- Once Bob receives and decrypts the key using the same custom library and his FPGA, both parties can use this key for encrypting and decrypting their messages. The complexity and unpredictability of the key generation process, coupled with the hardware-specific encryption for key sharing, ensure that the communication remains secure.

Python Example

```
Python Gate Example
Python Gate Example > No Selection
1 import numpy as np
2
3 def apply_phase_shift(qubit, phi):
4     """
5     Simulates applying a phase shift to a qubit.
6
7     Args:
8     - qubit: A numpy array representing the qubit state.
9     - phi: The phase shift angle in radians.
10
11     Returns:
12     - The qubit state after applying the phase shift.
13     """
14     # Phase shift matrix representation using cosine to simulate the effect
15     phase_shift_matrix = np.array([[1, 0], [0, np.cos(phi)]])
16
17     # Apply the phase shift to the qubit
18     return np.dot(phase_shift_matrix, qubit)
19
20 def main():
21     # Initial qubit state in superposition (for simplicity, we use real numbers to represent amplitudes)
22     qubit = np.array([1/np.sqrt(2), 1/np.sqrt(2)])
23
24     # Phase shift angle in radians (e.g., pi/4)
25     phi = np.pi / 4
26
27     # Apply the phase shift
28     qubit_after_phase_shift = apply_phase_shift(qubit, phi)
29
30     print("Initial qubit state:", qubit)
31     print("Qubit state after applying a phase shift of pi/4 radians:", qubit_after_phase_shift)
32
33 if __name__ == "__main__":
34     main()
35 |
36
```

Cracking The Encryption

```
CrackingThenEncryption
CrackingThenEncryption > No Selection
1 import numpy as np
2 |
3 def quantum_encrypt(message, key_phase):
4     """Simulates quantum encryption by applying a phase shift to the message."""
5     encrypted_message = np.exp(1j * key_phase) * message
6     return encrypted_message
7
8 def quantum_decrypt(encrypted_message, key_phase):
9     """Simulates quantum decryption by reversing the phase shift."""
10    decrypted_message = encrypted_message * np.exp(-1j * key_phase)
11    return decrypted_message
12
13 def eavesdropper_attempt(encrypted_message):
14    """An eavesdropper tries to decrypt the message without the quantum key."""
15    guessed_phase = np.random.uniform(0, 2*np.pi)
16    decrypted_attempt = encrypted_message * np.exp(-1j * guessed_phase)
17    return decrypted_attempt
18
19 # Quantum key (phase shift) known only to the sender and receiver
20 true_key_phase = np.pi / 4 # Example phase shift
21
22 # Simulate encrypting a message
23 original_message = np.array([1+0j]) # Simplified quantum "message"
24 encrypted_message = quantum_encrypt(original_message, true_key_phase)
25
26 # The receiver decrypts the message with the correct key
27 decrypted_message = quantum_decrypt(encrypted_message, true_key_phase)
28
29 # An eavesdropper attempts to decrypt the message without the key
30 eavesdropper_message = eavesdropper_attempt(encrypted_message)
31
32 # Compare the results
33 print("Original message:", original_message)
34 print("Decrypted message with correct key:", decrypted_message)
35 print("Eavesdropper's decryption attempt:", eavesdropper_message)
36
37
```



Don Golding

Space Exploration and Communication

- We could apply a similar library to communicate complex mathematical equations using your Polarfire RT to a space craft. You could almost and possibly do quantum simulations on mars to demonstrate its capability. It also could also be used for cryptography for satellite communication. Just a thought and not for sure if it would work.

Examples

- In these pseudocode examples, `mat!` would be a hypothetical Forth word used to initialize the matrices representing quantum gates, and `qubit*` would represent applying a gate to a qubit. The variables `qubit`, `qubit2`, and all the gate variables would store the state of the qubits and the matrices for the gates.

Pauli-X Gate (NOT Gate)

forth

 Copy code

```
variable pauli-x

: init-pauli-x ( -- )
  pauli-x mat!

: apply-pauli-x ( -- )
  qubit pauli-x qubit* ;
```

Pauli-Y Gate

forth

 Copy code

```
variable pauli-y

: init-pauli-y ( -- )
  pauli-y mat!

: apply-pauli-y ( -- )
  qubit pauli-y qubit* ;
```

Pauli-Z Gate (Phase Flip Gate)

forth

 Copy code

```
variable pauli-z


: init-pauli-z ( -- )
  pauli-z mat!

: apply-pauli-z ( -- )
  qubit pauli-z qubit* ;
```



Hadamard Gate

forth

 Copy code


```
variable hadamard

: init-hadamard ( -- )
  hadamard mat!

: apply-hadamard ( -- )
  qubit hadamard qubit* ;
```

T Gate (T-Phase Gate)

forth

 Copy code

```
variable t-gate

: init-t-gate ( -- )
  t-gate mat!

: apply-t-gate ( -- )
  qubit t-gate qubit* ;
```

CNOT Gate (Controlled-NOT Gate)

forth

 Copy code

```
variable cnot
variable qubit2

: init-cnot ( -- )
  cnot mat!

: init-qubit2 ( -- )
  qubit2 c!

: apply-cnot ( -- )
  qubit qubit2 cnot qubit* ;
```